

Hardy-Weinberg Principle Examples

A population has only 2 alleles, R and r , for a particular gene. The allele frequency for R is 30%. What are the frequencies of RR , Rr , and rr in the population?

$$P+q=1 \quad P^2+2pq+q^2=1$$

Known: $R = 30\%$
 R represented by P
 $\therefore P = 30\% \text{ or } 0.3$

find q : $P+q=1$
 $0.3+q=1-0.3$
 $q=0.7$

Solve for genotypic frequencies

$$\begin{aligned} RR(P^2) &= (0.3)^2 \\ &= 0.09 && \text{Check} \\ Rr(2pq) &= 2(0.3)(0.7) \\ &= 0.42 && 0.09 \\ rr(q^2) &= (0.7)^2 \\ &= 0.49 && + 0.42 \\ & && \hline & && 1 \end{aligned}$$

$$\begin{aligned} R &= 0.3 \\ r &= 0.7 \\ RR &= 0.09 \\ Rr &= 0.42 \\ rr &= 0.49 \end{aligned}$$

In a population of 200 mice, 8 have short tails, which is a recessive trait. The rest have long tails. Determine the frequencies of the genotypes and of the dominant and recessive alleles.

T = long tailed
 t = short tailed $P+q=1 \quad P^2+2pq+q^2=1$

Known: $tt = \frac{8}{200} = 0.04$
 tt is q^2

find q :
 $q^2 = 0.04$
 $q = \sqrt{0.04} = 0.2$

find p :
 $P+q=1$

$$\begin{aligned} P+0.2 &= 1 \\ P &= 1-0.2 \\ P &= 0.8 \end{aligned}$$

Solve for genotypic frequencies

$$\begin{aligned} TT(P^2) &= (0.8)^2 \\ &= 0.64 \end{aligned}$$

$$\begin{aligned} Tt(2pq) &= 2(0.8)(0.2) \\ &= 0.32 \end{aligned}$$

$$tt(q^2) = 0.04$$

$$\begin{aligned} T &= 0.8 \\ t &= 0.2 \end{aligned}$$

$$\begin{aligned} TT &= 0.64 \\ Tt &= 0.32 \\ tt &= 0.04 \end{aligned}$$

Check

$$\begin{aligned} TT &= 0.64 \\ Tt &= 0.32 \\ tt &= 0.04 \end{aligned} \quad \begin{array}{l} \checkmark \\ \checkmark \end{array}$$